

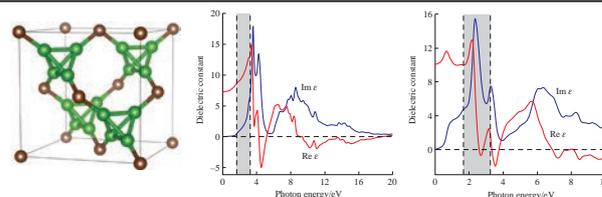
Quantum chemical modeling of solid-state B_4X structures containing tetrahedral B_4 units with $X = B, C, Al, Si$

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The quantum chemical modeling of new solid state structures based on a diamond lattice in which pairs of carbon atoms are replaced by B_4X fragments (where B_4 is a tetrahedron and X are B, C, Al or Si atoms) has been performed using density functional calculations.



The acquisition of new materials with unusual structures for micro- and nanoelectronics is a problem of modern materials science. An important role in the search for these materials and underlying basic substances belongs to computational design,^{1–3} which is efficient for the prediction and theoretical characterization of various crystalline forms of carbon⁴ and new allotropic forms of boron.^{5–10} Previously, by analogy with supertetrahedral carbon (T-carbon, dia-a and their motifs and so on),^{11–13} we have proposed supertetrahedral boron as a new allotropic form of boron.^{8–10} As an electron-deficient element, boron is enforced to use multi-center bonds in order to form polyatomic crystalline structures, which not only are lighter than carbon-based analogs but also can have other attractive physical and chemical properties (hardness, electrical conductivity or semiconducting properties, etc.).

Here, we computationally studied the geometric and electronic structures of solids constructed on the basis of a diamond lattice in which pairs of neighboring carbon atoms are replaced by the fragments B_4-X ($X = B, C, Al, Si$) using density functional theory (DFT) quantum chemical calculations with imposing periodic boundary conditions. The corresponding crystal structures are denoted as $cF-B_4X$. The calculations were carried out using the Vienna *ab initio* Simulations Package (VASP)^{14–17} with PAW pseudopotentials^{18,19} and the PBEsol exchange-correlation functional.²⁰ The plane-wave cutoff energy of 750 eV of the associated pseudopotentials was used. The Brillouin zone was sampled by the Monkhorst–Pack method²¹ with an automatically generated grid $25 \times 25 \times 25$. The convergence criteria for total energies and forces on atoms were 10^{-8} eV per atom and 10^{-6} eV \AA^{-1} , respectively. The unit cell of $cF-B_4X$ was plotted using the VESTA software.²²

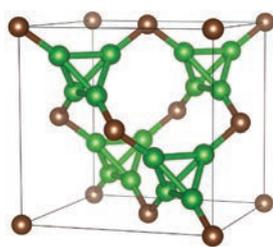


Figure 1 Conventional unit cell of the supertetrahedral crystal structure of $cF-B_4X$. Boron tetrahedrons and X atoms are shown green and brown, respectively.

Table 1 Calculated lattice constants a , Wyckoff position coordinates x for B atoms, X–B bond lengths d_1 , B–B bond lengths d_2 , density ρ and cohesive energy E_{coh} for $cF-B_4X$ ($X = B, C, Al, Si$) structures.

Structure	$a/\text{\AA}$	x	$d_1/\text{\AA}$	$d_2/\text{\AA}$	$\rho/\text{g cm}^{-3}$	$E_{\text{coh}}/\text{eV per atom}$
$cF-B_5$	6.255	0.15304	1.658	1.715	1.47	–5.75
$cF-B_4C$	6.003	0.15042	1.564	1.691	1.70	–6.50
$cF-B_4Al$	7.321	0.16784	2.128	1.701	1.19	–4.75
$cF-B_4Si$	6.995	0.16465	1.995	1.689	1.38	–5.47

The crystal structures of $cF-B_4X$ have a face-centered cubic lattice with four B atoms and one X atom in the primitive unit cell (Figure 1). The space group is $F\bar{4}3m$ (number 216). Atoms X occupy the Wyckoff position $4a$ with the coordinates (0, 0, 0), and atoms B occupy the Wyckoff position $16e$ with the coordinates (x, x, x) . All the structures have a negative cohesive energy (Table 1); therefore, they are thermodynamically stable.

According to the calculations of the phonon spectra of four structures, which are shown in Figures 2, 3 and S1–S2 (Online Supplementary Materials), only two of them with $X = C$ and $X = Si$ between boron tetrahedrons possess dynamic stability. With $X = B$ and $X = Al$ atoms, the systems are dynamically unstable; therefore, their properties have not been studied. The geometric characteristics of solids found by the calculations are given in Table 1. According to the calculations, the length of the intra-tetrahedral B–B bond is 1.689–1.715 \AA (Table 1), which is close to that (1.680 \AA determined by X-ray crystallography²³) of a similar bond in B_4Cl_4 . According to the NBO²⁴ and AdNDP²⁵ analyzes, these in tetrahedron B–B bonds represent three-center two-electron ($3c-2e$) bonds. The B–X bonds in all of the compounds conform to the two-electron two-center ($2c-2e$) bonds and, in terms of the NBO theory, correspond to covalent bonds. The calculated lengths of the B–C bonds in the $cF-B_4C$ structure are 1.564 \AA , which is close to the lengths of similar bonds in *closo*-carboranes^{26–29} and super-tetrahedral carboranes.¹⁰ The length of the covalent B–Si bond in the $cF-B_4Si$ structure is 1.995 \AA , which is close to the calculated length of such a bond in a silicon cluster (~ 1.88 – 2.09 \AA) doped with a boron atom³⁰ and a two-dimensional borosilicon flat sheet.³¹ The calculations of the electronic band structures of the test compounds showed that the $cF-B_4C$ and $cF-B_4Si$ systems are semiconductors (Figures 4 and 5). Both systems have a small band gap between the valence and

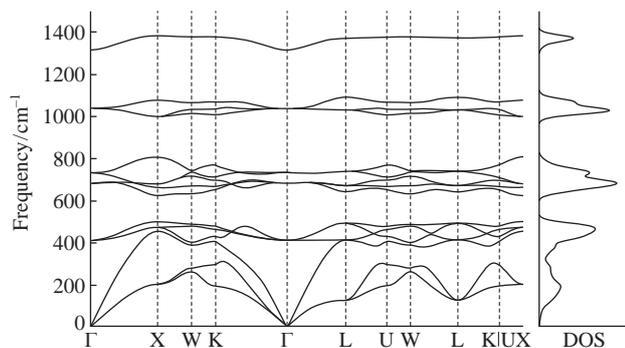


Figure 2 Calculated phonon dispersion curves along high-symmetry lines in the first Brillouin zone (left) and phonon density of states (right) for *cF-B₄C*.

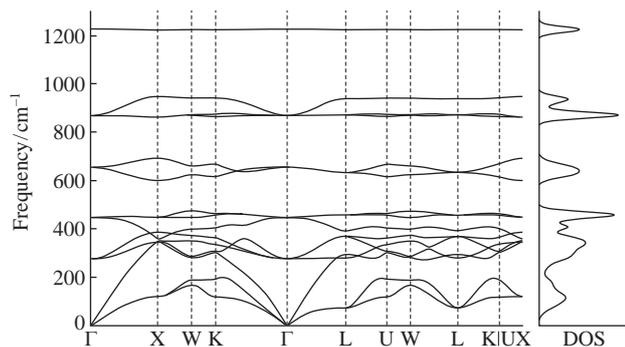


Figure 3 Calculated phonon dispersion curves along high-symmetry lines in the first Brillouin zone (left) and phonon density of states (right) for *cF-B₄Si*.

conduction bands, which in the case of silicon decreases to 0.62 eV.

The calculated values of elastic constants, bulk modulus, shear modulus, Young's modulus and Poisson's ratio for *cF-B₄C* and *cF-B₄Si* structures are given in Table 2. For both the struc-

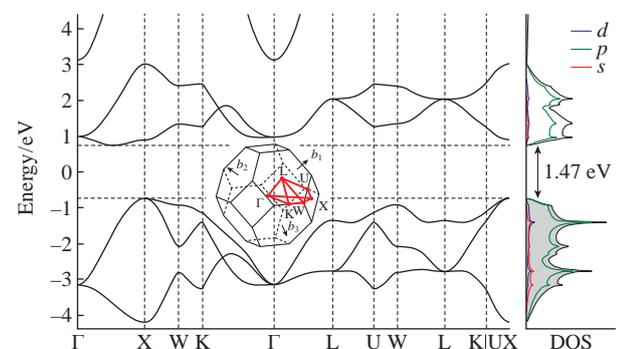


Figure 4 Calculated electronic band structure along high-symmetry lines in the first Brillouin zone (left) and electronic density of states (right) for *cF-B₄C*.

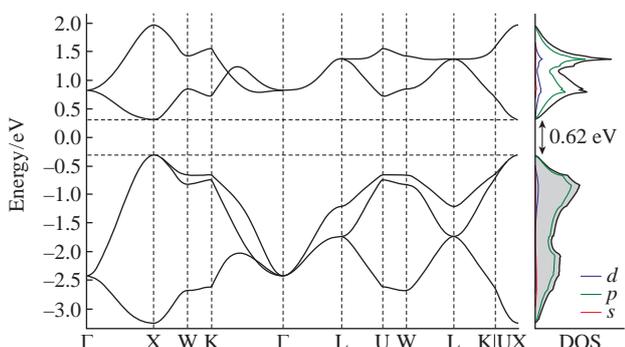


Figure 5 Calculated electronic band structure along high-symmetry lines in the first Brillouin zone (left) and electronic density of states (right) for *cF-B₄Si*.

Table 2 Calculated elastic constants c_{ij} , bulk modulus K , shear modulus G , Young's modulus E and Poisson's ratio ν for *cF-B₄C* and *cF-B₄Si*.

Structure	c_{11} /GPa	c_{12} /GPa	c_{44} /GPa	K /GPa	G /GPa	E /GPa	ν
<i>cF-B₄C</i>	201.57	121.86	50.50	148.43	45.93	124.91	0.3597
<i>cF-B₄Si</i>	109.97	66.87	25.79	81.24	24.00	65.56	0.3655

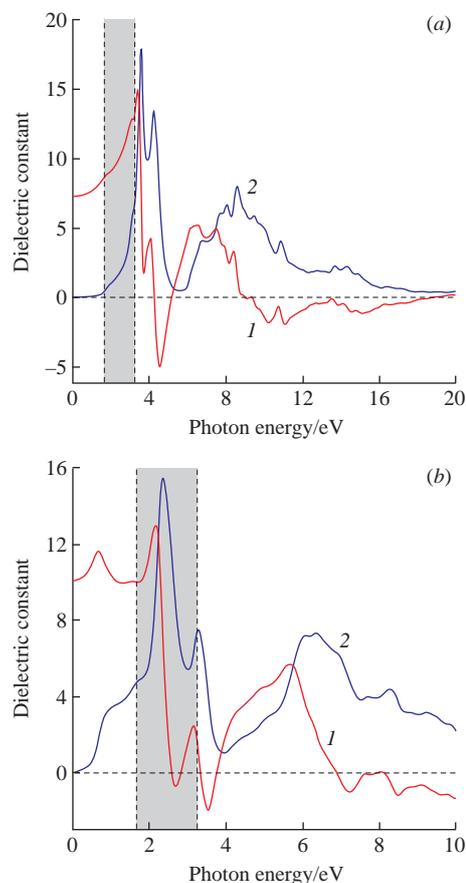


Figure 6 Frequency dependence of the (1) real and (2) imaginary parts of complex dielectric permittivity for (a) *cF-B₄C* and (b) *cF-B₄Si*.

tures, the bulk and shear modulus values are smaller than those of super-tetrahedral carbon ($K = 169$ GPa, $G = 70$ GPa)¹² but greater than those of super-tetrahedral boron ($K = 68$ GPa, $G = 16$ GPa).⁸ The bulk modulus for the *cF-B₄Si* structure is smaller than that of crystalline silicon.³² The elastic constants of *cF-B₄C* and *cF-B₄Si* suggest high plasticity of the materials.

The dependences of the real and imaginary parts of the dielectric constants on photon energy for the two structures are illustrated in Figure 6. For the *cF-B₄C* structure, the longest wavelength absorption is found in the near UV spectral region with band maxima at 350 nm. For the *cF-B₄Si* structure, the longest wavelength absorption lies in the visible spectral region with band maxima at 530 nm.

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Online Supplementary Materials

Supplementary data associated with this article can be found in the online version at doi: 10.1016/j.mencom.2018.03.021.

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